AMS-Net: Adaptive Multi-Scale Network for Image Compressive Sensing

Kuiyuan Zhang[®], Zhongyun Hua[®], *Member, IEEE*, Yuanman Li[®], *Member, IEEE*, Yongyong Chen[®], *Member, IEEE*, and Yicong Zhou[®], *Senior Member, IEEE*

Abstract-Recently, deep convolutional neural networks have been applied to image compressive sensing (CS) to improve reconstruction quality while reducing computation cost. Existing deep learning-based CS methods can be divided into two classes: sampling image at single scale and sampling image across multiple scales. However, these existing methods treat the image low-frequency and high-frequency components equally, which is an obstruction to get a high reconstruction quality. This paper proposes an adaptive multi-scale image CS network in wavelet domain called AMS-Net, which fully exploits the different importance of image low-frequency and high-frequency components. First, the discrete wavelet transform is used to decompose an image into four sub-bands, namely the low-low (LL), low-high (LH), high-low (HL), and high-high (HH) sub-bands. Considering that the LL sub-band is more important to the final reconstruction quality, the AMS-Net allocates it a larger sampling ratio, while allocating the other three sub-bands a smaller one. Since different blocks in each sub-band have different sparsity, the sampling ratio is further allocated block-by-block within the four sub-bands. Then a dual-channel scalable sampling model is developed to adaptively sample the LL and the other three sub-bands at arbitrary sampling ratios. Finally, by unfolding the iterative reconstruction process of the traditional multi-scale block CS algorithm, we construct a multi-stage reconstruction model to utilize multi-scale features for further improving the reconstruction quality. Experimental results demonstrate that the proposed model outperforms both the traditional and state-of-the-art deep learning-based methods.

Index Terms—Compressive sensing, convolutional neural networks, discrete wavelet transform, block compressive sampling.

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Kuiyuan Zhang, Zhongyun Hua, and Yongyong Chen are with the School of Computer Science and Technology, Harbin Institute of Technology, Shenzhen, Shenzhen 518055, China (e-mail: zkyhitsz@gmail.com; huazyum@gmail.com; yongyongchen.cn@gmail.com).

Yuanman Li is with the College of Electronics and Information Engineering, Shenzhen University, Shenzhen 518060, China (e-mail: yuanmanli@ szu.edu.cn).

Yicong Zhou is with the Department of Computer and Information Science, University of Macau, Macau 999078, China (e-mail: yicongzhou@um.edu.mo). Digital Object Identifier 10.1109/TMM.2022.3198323

I. INTRODUCTION

C OMPRESSIVE sensing (CS) is a new signal acquisition technique [1], [2]. It can sample a signal using a measurement matrix at a far lower ratio than the requirement of Nyquist sampling theory and can construct the original signal from its measurements [3]. Because the sampling and compressing operations are performed simultaneously, the CS shows good performance in data acquisition, storage, and transmission [4], [5]. Researchers have applied the CS theory to many fields such as magnetic resonance imaging [6], video compression [7], image coding [8] and snapshot compressive imaging [9].

There are two main tasks in studying the CS: signal sampling and signal reconstruction. For traditional CS schemes, although their measurement matrices can satisfy the restricted isometry property [10], they have low reconstruction performance due to the lack of adaptability for signals with different features. Besides, their reconstruction algorithms [11], [12], [13] were developed by considering the prior knowledge of the original signal and applying iterative non-linear optimization approaches for reconstruction. These reconstruction algorithms have some disadvantages such as low reconstruction quality, high complexity, and blocking artifacts.

Recently, some deep learning-based image CS models have been proposed to solve the limitations of traditional CS methods. These models implement the reconstruction process using the convolutional neural networks (CNNs) to replace the time-consuming optimization process, and their measurement matrices can be learned adaptively [14], [15], [16], [17]. Besides, some works first decompose an image using different multi-scale decomposition approaches and then sample these decomposed images across scales to sufficiently utilize the multi-scale features [18], [19], [20]. Compared with traditional iterative optimization-based algorithms, these deep learning-based methods can significantly improve the reconstruction quality and reduce the time complexity of reconstruction. However, these methods directly sample images at single scale [14], [15], [16], [17] or across multiple scales [18], [19], [20] by equally treating the image low-frequency and high-frequency components with the same resources. This limits the reconstruction quality, since the low-frequency components are more important to the reconstruction quality of an image than the high-frequency components, especially at a low sampling ratio [12].

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In this paper, we propose a wavelet domain-based adaptive multi-scale image CS network (AMS-Net) by considering the different importance of the image low-frequency and high-frequency components. It can adaptively sample images in the multi-scale domain. Specifically, the discrete wavelet transform (DWT) is used to decompose an image from the spatial domain to the frequency domain, generating the low-low (LL), low-high (LH), high-low (HL), and high-high (HH) sub-bands. Considering that the LL sub-band is the low-frequency components and is more important to the reconstruction quality than the other three sub-bands, we design a dual-channel scalable sampling model that assigns the LL sub-band a larger sampling ratio while assigning the other three sub-bands a smaller one. As different blocks in the sub-bands have different sparsity, we apply a linear sampling resource assigning (LSRA) strategy to these two channels to further adjust the sampling ratios according to block sparsity. By unfolding the reconstruction process of the multi-scale block CS (MS-BCS) strategy [12] using CNN, we construct a multi-stage reconstruction architecture. In each stage, the reconstruction model first applies a dual-channel projection operation in the wavelet domain on the reconstructed image block-by-block, and then implements a full-image denoising operation in the spatial domain to remove the noise and blocking artifacts.

The contributions and novelty of this paper are summarized as follows:

- We present a wavelet domain-based adaptive multi-scale image CS network, which is the first deep learning-based CS network that considers the different importance of image low-frequency and high-frequency components.
- We develop an LSRA strategy to adjust the sampling ratios according to block sparsity and propose a dual-channel scalable sampling model to perform the adaptive sampling tasks at arbitrary sampling ratios.
- Unfolding the traditional reconstruction strategy with CNN, we design a multi-stage reconstruction architecture to exploit the multi-scale features, which can further improve the reconstruction quality.
- We conduct a comprehensive evaluation and the results show that our model outperforms both the traditional and state-of-the-art deep learning-based CS methods.

The rest of this paper is organized as follows. Section II introduces the CS theory and the traditional MS-BCS algorithm. Section III reviews the deep learning-based CS models. Section IV presents the network structure of our AMS-Net. Section V evaluates the performance of the proposed model and compares it with state-of-the-art methods. Section VI gives a conclusion of this paper.

II. PREREQUISITE KNOWLEDGE

A. Compressive Sensing

For a given measurement matrix $\mathbf{\Phi} \in \mathbb{R}^{m \times n}$ with $n \gg m$, the CS theory specifies that the sparse signal $\mathbf{x} \in \mathbb{R}^{n \times 1}$ can be sampled as $\mathbf{y} = \mathbf{\Phi}\mathbf{x}$ and it can be reconstructed using some reconstruction algorithms [11], [13] from the measurements $\mathbf{y} \in \mathbb{R}^{m \times 1}$. The CS methods can be divided into two classes: single-scale CS methods and multi-scale CS methods. The single-scale CS methods sample and reconstruct images in the spatial domain, while the multi-scale CS methods sample images in the multi-level decomposition domain or reconstruct images using multi-scale information.

B. Multi-Scale Block Compressive Sensing

When processing a two-dimensional (2D) image, the size of the measurement matrix will be quite large if transforming the 2D image into a one-dimensional (1D) signal. To solve this problem, block-based sampling (BCS) methods [12], [21] have been widely used to separately sample each non-overlapping image block with constant size $B \times B$.

Let x_i represent the 1D vector transformed from the *i*-th block of the image **X**, and the sampling process is written as

$$y_i = \Phi_B x_i, \tag{1}$$

where $\Phi_B \in \mathbb{R}^{n_B \times B^2}$ is a measurement matrix and $y_i \in \mathbb{R}^{n_B \times 1}$ is the measurements of x_i . The sampling ratio (sr) is $sr = n_B/B^2$. The authors in [21] proposed a BCS-SPL method that directly samples image blocks in the spatial domain and uses projected Landweber reconstruction mechanism to reduce blocking artifacts. To utilize the multi-scale features of images, the authors in [12] further proposed the MS-BCS to deploy the BCS-SPL in the multi-level decomposition domain.

1) Multi-Scale Sampling: To sample an image in multi-scale domain, one should first decompose the image to produce L levels of wavelet decomposition coefficients. Then each block $\tilde{\mathbf{x}}_{l,s,i}$ of a sub-band s at level l is sampled as

$$\mathbf{y}_{l,s,i} = \mathbf{\Phi}_l \tilde{\mathbf{x}}_{l,s,i},\tag{2}$$

where $s \in \{LH, HL, HH\}$, $1 \le l \le L$ and Φ_l means the measurement matrix for the level *l*. Since a lower level of the decomposition coefficients is more important to the final reconstruction quality, the sampling resources are adaptively adjusted for each level *l*.

2) *Multi-Scale Reconstruction:* First, the initial estimation of each image block is generated by linearly mapping the measurements, which is shown as

$$\hat{x}_{l,s,i}^{(0)} = \mathbf{\Phi}_l^* y_{l,s,i},\tag{3}$$

where Φ_l^* represents the linear mapping matrix and it is the pseudo-inverse matrix of Φ_l . Then the reconstruction process is an iterative process and each iterative step contains the following two operations.

• Projection in the wavelet domain: This operation is to find a vector that is closer than the current vector $\hat{x}_{l,s,i}^{(t)}$ on the hyperplane $\mathbf{H} = {\hat{x}_{l,s,i} : \Phi_l \hat{x}_{l,s,i} = y_{l,s,i}}$. The projection operation is defined as

$$\hat{x}_{l,s,i}^{(t+1)} = \hat{x}_{l,s,i}^{(t)} + \Phi_l^* \left(y_{l,s,i} - \Phi_l \hat{x}_{l,s,i}^{(t)} \right)$$
$$= \hat{x}_{l,s,i}^{(t)} + \hat{x}_{l,s,i}^{(0)} - \Phi_l^* \Phi_l \hat{x}_{l,s,i}^{(t)}.$$
(4)

• *Deblocking and Denoising:* Block-based reconstruction and projection may generate some blocking artifacts and



Fig. 1. The framework of the AMS-Net. The X donates the original image and the $\hat{\mathbf{X}}^{(T)}$ represents the reconstructed image.

noises. Thus, a non-linear mapping

$$\hat{\mathbf{X}}^{(t+1)} = \mathcal{H}\left(\hat{\mathbf{X}}^{(t+1)\prime}\right)$$
(5)

is employed to remove the blocking artifacts and noises of the reconstructed image $\hat{\mathbf{X}}^{(t+1)\prime}$, where \mathcal{H} donates the Wiener filtering in the spatial domain or the thresholding operation in the frequency domain, and $\hat{\mathbf{X}}^{(t+1)\prime}$ is the full image generated by applying inverse DWT (IDWT) to the reconstructed blocks $\hat{x}_{l,s,i}^{(t+1)}$.

III. DEEP LEARNING-BASED CS METHODS

Since deep learning-based methods can show great effect in image restoration tasks, they were used to solve the signal sampling and reconstruction problems [14], [15], [22], [23], [24]. The authors in [22] proposed the first model that uses an stacked denoising autoencoder to reconstruct the image patches from the sampled measurements. Later, the authors in [23] constructed a deep CNN architecture to implement the non-iterative reconstruction process from the sampled measurements. However, the two works use constant measurement matrices to sample images. This limits the reconstruction quality because the constant measurement matrices may lose the generality and adaptability for images with different features. Thus, some models were proposed to simultaneously train the sampling network and reconstruction network [14], [15], [24]. For example, the CSNet^{*} [24] and CSNet⁺ [14] use learnable convolutional layers without overlapping to mimic the sampling process. Then the measurements are transmitted into the reconstruction network to get the final reconstructed image. All these models are single-scale CS methods and they apply sampling and reconstruction in the spatial domain.

To utilize the multi-scale features in the deep learning-based CS methods, the models LAPRAN [25] and SCSNet [16] divide CS measurements into multiple levels. The CS measurements at the lowest level are used to generate the initial reconstruction of the image, while those at higher levels are progressively fused to generate a high-frequency image residual for enhancing the quality of the initial reconstruction. Besides, the model MSR-Net [17] applies three parallel channels with different convolution kernel sizes in the reconstruction stage to fuse multi-scale features. The models in [16], [17], [25] exploit multi-scale features in the reconstruction stage but still sample images at single scale in the spatial domain. To directly learn multi-scale features in the sampling stage, the model MS-DCSNet [18]

samples the decomposed images block-by-block across multiple wavelet scales. Moreover, it integrates a multi-level wavelet convolutional neural network to further utilize the multi-scale information in the reconstruction stage. Using the same reconstruction architecture but different multi-scale decomposition methods with the MS-DCSNet [18], the models DoC-DCS [19], SS-DCI [20] and P-DCI [20] also develop multi-scale CS architectures to utilize multi-scale features in both the sampling and reconstruction stages. Specifically, the multi-scale decomposition methods in the models DoC-DCS [19], SS-DCI [20] and P-DCI [20] are the difference of convolution, scale-space and pyramid, respectively.

These existing single-scale and multi-scale deep learningbased CS methods equally treat the image low-frequency and high-frequency components by sampling them using the same resources. However, the low-frequency components are usually more important to the final reconstruction quality than the highfrequency components [12]. Sampling the image low-frequency and high-frequency components equally may lead to a low reconstruction quality, especially at low sampling ratios.

IV. AMS-NET

In this section, we present the AMS-Net and Fig. 1 shows its framework. It is an end-to-end structure that contains a dualchannel sampling model and a multi-stage reconstruction model. To demonstrate the sampling and reconstruction processes, we assume that the input image is $\mathbf{X} \in \mathbb{R}^{2H \times 2W \times 1}$, and the image block size is $B \times B$.

A. Sampling Model

The framework of the sampling model is shown as Fig. 2. The original image \mathbf{X} is decomposed by DWT and then sampled by a dual-channel scalable sampling model with LSRA strategy.

1) DWT Decomposition: We use the DWT to decompose the original image X into four sub-figures, namely the LL, LH, HL and HH sub-bands, and each sub-band is of size $\mathbb{R}^{H \times W \times 1}$. Because the image low-frequency and high-frequency components have different importance to the final reconstruction quality, we use different sampling ratios to sample them. Specifically, we set the LL sub-band as the first channel and denote it as $\mathbf{P} \in \mathbb{R}^{H \times W \times 1}$, and set the LH, HL and HH sub-bands as the second channel and denote it as $\mathbf{Q} \in \mathbb{R}^{H \times W \times 3}$.

Assuming that the target sampling ratio of the input image X is sr, we set the sampling ratio in sub-band P as sr_p and that in sub-bands Q as sr_q . The sr, sr_p and sr_q should satisfy the



Fig. 2. The sampling model of the AMS-Net. The original image \mathbf{X} is decomposed by DWT to generate LL, LH, HL and HH sub-bands. A dual-channel architecture is used to assign sampling resources for sampling the LL sub-band and the other three sub-bands. The \mathbf{Y}_1 and \mathbf{Y}_2 denote the measurements of the LL sub-band and the other three sub-bands, respectively.

following equation:

$$sr = \frac{sr_p \times HW + sr_q \times 3HW}{2H \times 2W}$$
$$= \frac{1}{4}sr_p + \frac{3}{4}sr_q \qquad . \tag{6}$$

Let the allocation ratio $ar = \frac{sr_p \times HW}{sr \times 2H \times 2W} = \frac{sr_p}{4sr}$ represent the ratio of the measurement number in **P** to the total measurement number in X. Then one can obtain that $sr_p = 4sr \times ar$ and $sr_q = \frac{4sr \times (1-ar)}{3}$. When sr is very low, the low-frequency components are critical, and we set a large ar to reconstruct more image approximations. When sr is high, the high-frequency components become important, and we set a relatively small ar to reconstruct more image details. Besides, from the global view, the low-frequency components are more important to the final reconstruction quality than the high-frequency components, since the image approximations contain most of the image information [12]. Thus, the ar should be not smaller than 0.25 to ensure that $sr_p \geq sr_q$.

2) LSRA Strategy: The sampling resources are linearly assigned according to the block sparsity in P and Q, respectively. Specifically, the saliency information [26] is used to measure the block sparsity. The larger saliency information indicates that the corresponding image block is less sparse and thus should be assigned more sampling resources.

For \mathbf{P} , its saliency map [26] is defined as:

$$D = \operatorname{sign}(C_t(\mathbf{P})),$$

$$F = \operatorname{abs}\left(C_t^{-1}(D)\right),$$

$$\mathbf{S} = G * F^2,$$
(7)

where C_t and C_t^{-1} are the 2D discrete cosine transform and its inverse transform, respectively, and G is a 2D Gaussian low-pass filter. To smooth the calculation results, we further normalize the values of **S** into [0, 1]. Assume that $\mathbf{P}_{ij} \in \mathbb{R}^{B \times B \times 1}$ represents an image block in **P**, where $i \in \{1, 2, ..., h\}$ and $j \in \{1, 2, \dots, w\}$ with h = H/B and w = W/B. The quantified saliency information \mathbf{v}_{ij} of each image block \mathbf{P}_{ij}



(a) Sampling ratio = 0.1

Illustration of the measurement allocation map. The first row shows the Fig. 3. LL coefficients of the two images and the second row shows their measurement allocation maps.

is calculated as

$$\mathbf{v}_{ij} = \sum_{s \in \mathbf{S}_{ij}} s / \sum_{s \in \mathbf{S}} s,\tag{8}$$

where S_{ij} is the corresponding region of P_{ij} in S, and $\sum_{i=1}^{h} \sum_{j=1}^{w} \mathbf{v}_{ij} = 1$. For simplicity, we assume that the subbands \mathbf{P} and \mathbf{Q} have the same saliency information distribution within blocks.

Algorithm 1 shows the linear sampling resource assigning process. We first initialize the measurements for each image block to avoid the final number of measurements of some blocks being too small, and then linearly assign the rest sampling resources according to the saliency information. Using Algorithm 1 with two group of inputs $\{\mathbf{v}, sr_p, B, (H, W, 1)\}$ and $\{\mathbf{v}, sr_{\underline{q}}, B, (H, W, 3)\},$ we can obtain the measurement number m_{ij}^p for each image block \mathbf{P}_{ij} and measurement number m_{ij}^q for each image block \mathbf{Q}_{ij} , respectively. Note that the actual total measurements are less than the target total measurements because of the floor function in Algorithm 1. Then we use these reserved sampling resources to save the saliency information v and include it in the actual sampling results. Due to the errors that may be caused by the floor operation, the actual sampling ratio (sr_a) and target sampling ratio (sr_t) may have some slight difference. Table I lists the average errors between the sr_a and sr_t for images in Set11 at different sampling ratios.

To illustrate the advantage of our adaptive sampling, we present the measurement allocation maps in the LL coefficients of two images "Cameraman" and "Parrots" in Fig. 3. The image block size is set as 16×16 . Each value indicates the measurement number to the image block and a larger value means more allocated measurement resources. It can be seen that the image blocks with more details are allocated more measurement resources. For example, the camera in the image "Cameraman"

Target sr	0.01	0.03	0.05	0.1	0.2	0.3	0.4	0.5
$sr_a - sr_t$	$+9e^{-4}$	$+8e^{-5}$	$+6e^{-6}$	$-6e^{-6}$	$+3e^{-5}$	$+1e^{-4}$	$+1e^{-4}$	$-2e^{-4}$
$(sr_a - sr_t)/sr_t$	9.58%	0.23%	0.006%	-0.01%	0.01%	0.05%	0.03%	-0.02%

Algorithm 1: The LSRA Strategy.

Input: Saliency information v, sampling ratio sr', block size B, image size (H, W, C)**Output:** The measurement number \mathbf{m}_{ij} for each image block 1: $pixels_per_block = B \times B \times C$ $total = |sr' \times H \times W \times C|$ 2: $base = [sr'/3 * pixels_per_block]$ 3: 4: $rest = total - (base \times \frac{H}{B} \times \frac{W}{B})$ for $i = 1 : \frac{H}{B}$ do 5: for $j = 1 \stackrel{D}{:} \frac{W}{B}$ do 6: $\mathbf{m}_{ij} = base + |rest \times \mathbf{v}_{ij}|$ 7: 8: end for

and the eyes in the image "Parrots" have more details, and thus their related image blocks are allocated more measurement resources.

3) Dual-Channel Scalable Sampling: Following existing deep learning-based CS methods [14], [15], we also use the BCS strategy to reduce the memory and computational burden rather than directly sampling the whole image. When applying different sampling ratios to different image blocks, one usually constructs a measurement matrix for each sampling ratio and this will highly increase the parameter number of the model. To solve the problem, we apply a scalable deep compressive sensing method that can perform different sampling tasks with only one measurement matrix. The convolution operation is used to mimic the compressive sampling process on the image block-by-block. Note that our method samples image blocks without overlapping, and thus the kernels of each convolution layer have the same size as the image block.

Specifically, to sample **P** with an adaptive sampling ratio, we replace the measurement matrix with a convolutional layer \mathcal{A}_1 with weights $w_{\mathcal{A}_1} \in \mathbb{R}^{B^2 \times (B \times B \times 1)}$, and the scalable sampling process is defined as

$$\mathbf{Y}_1 = (\mathcal{A}_1 * \mathbf{P}) \odot \mathbf{M}_{\mathcal{A}_1},\tag{9}$$

where * denotes the convolution operation with stride size $B \times B$, \odot represents the element-wise multiplication, $\mathbf{M}_{\mathcal{A}_1} \in \mathbb{R}^{h \times w \times B^2}$ is the mask to control the activities of measurements for each image block and $\mathbf{Y}_1 \in \mathbb{R}^{h \times w \times B^2}$ is the final sampling results. For each sub-tensor of the mask $\mathbf{M}_{\mathcal{A}_1}$, $\mathbf{M}_{\mathcal{A}_1} [i, j, 1 : m_{ij}^p] = 1$ and other elements are zeros. Thus, for the measurements of the image block \mathbf{P}_{ij} , only $\mathbf{Y}_1 [i, j, 1 : m_{ij}^p]$ are valid measurements and $\mathbf{Y}_1 [i, j, m_{ij}^p + 1 : B^2] = 0$. Similarly, using a convolutional layer \mathcal{A}_2 with weights $w_{\mathcal{A}_2} \in \mathbb{R}^{3B^2 \times (B \times B \times 3)}$, the sampling process for **Q** is calculated as

$$\mathbf{Y}_2 = (\mathcal{A}_2 * \mathbf{Q}) \odot \mathbf{M}_{\mathcal{A}_2},\tag{10}$$

where $\mathbf{M}_{\mathcal{A}_2} \in \mathbb{R}^{h \times w \times 3B^2}$ is the corresponding sampling mask and $\mathbf{Y}_2 \in \mathbb{R}^{h \times w \times 3B^2}$ is the sampling results of \mathbf{Q} . For each sub-tensor of the mask $\mathbf{M}_{\mathcal{A}_2}$, $\mathbf{M}_{\mathcal{A}_2} [i, j, 1 : m_{ij}^q] = 1$ and other elements are zeros. Thus, for the measurements of the image block \mathbf{Q}_{ij} , only $\mathbf{Y}_2 [i, j, 1 : m_{ij}^q]$ are valid measurements and $\mathbf{Y}_2 [i, j, m_{ij}^q + 1 : 3B^2] = 0$.

Formally, the whole sampling process can be expressed as

$$\mathbf{Y}_1, \mathbf{Y}_2 = f_{samp}(\mathbf{X}, sr, \mathcal{A}_1, \mathcal{A}_2).$$
(11)

To ensure that each image block has at least one measurement, $\frac{hw}{HW}$ and $\frac{hw}{3HW}$ are the smallest sampling ratios that the sampling model can perform on **P** and **Q**, respectively. Thus, the target sampling ratio of the input image should be not smaller than $\frac{hw}{2HW}$. When the target sampling ratio is smaller than this threshold, we set it as the threshold.

B. Reconstruction Model

We construct the reconstruction model by unfolding the reconstruction process of the traditional MS-BCS method. In the traditional MS-BCS method, the matrix Φ_l^* in (3) and (4) is the pseudo-inverse matrix of Φ_l . However, since the measurement matrix in our method is generated using learning strategy, the measurement matrix is not orthogonal in the training process, and the real-time calculation of pseudo-inverse will interrupt the backward propagation of gradients. Thus, for simplicity, we set the matrix Φ_l^* learnable in (3) and (4) to ensure that the model can be trained.

To improve the denoising and deblocking ability, we use a feed-forward learnable denoising block to replace the traditional denoising method in (5). This can also solve the problem that traditional denoising algorithms cannot propagate backward gradients in the training process. The full-image denoising and deblocking operation is expressed as

$$\hat{\mathbf{X}}^{(t+1)} = \mathbf{X}^{(t+1)\prime} + \mathcal{D}\left(\mathbf{X}^{(t+1)\prime}\right),\tag{12}$$

where \mathcal{D} indicates the denoising block containing convolutional layers. The residual learning is used to speed up the training process and improve the reconstruction performance.

The reconstruction model is shown as Fig. 4 and it contains an initial reconstruction module f_{init} and a deep reconstruction module f_{deep} . The original image can be reconstructed from its dual-channel measurements.

1) Initial Reconstruction: Our module f_{init} applies the initial reconstruction illustrated in (3) on the sampled measurements in the wavelet domain. Similar to the sampling module,

9:

end for



Fig. 4. The reconstruction model of the AMS-Net. The initial reconstruction image $\hat{\mathbf{X}}^{(0)}$ is generated by first linearly mapping the measurements \mathbf{Y}_1 and \mathbf{Y}_2 and then performing IDWT to the mapping results. Then the deep reconstruction module processes $\hat{\mathbf{X}}^{(0)}$ for T stages to obtain the final reconstructed image $\hat{\mathbf{X}}^{(T)}$. A dual-channel projection operation and a full-image denoising operation are used in each stage, in which the dual-channel projection is performed in the wavelet domain while the denoising operation is performed in spatial domain using d convolutional layers.

the learnable convolutional layers are used to implement the linear mapping matrix to get the initial reconstruction. Specifically, the measurements \mathbf{Y}_1 in the first channel is connected to a convolutional layer \mathcal{A}_1^* containing B^2 kernels of size $1 \times 1 \times B^2$. A tensor of size $\mathbb{R}^{h \times w \times B^2}$ is generated by convolving these B^2 kernels on the \mathbf{Y}_1 with stride size 1×1 . By reshaping the tensor into hw feature maps of size $B \times B \times 1$ and concatenating them into an $H \times W \times 1$ feature map, the initial reconstruction $\hat{\mathbf{P}}^{(0)}$ of \mathbf{P} in the first channel can be generated. Using the similar operation, the initial reconstruction $\hat{\mathbf{Q}}^{(0)}$ of \mathbf{Q} in the second channel can be obtained by connecting the measurements \mathbf{Y}_2 to a convolutional layer \mathcal{A}_2^* with $3B^2$ kernels of size $1 \times 1 \times 3B^2$.

The process of the initial reconstruction can be expressed as

$$\begin{cases} \hat{\mathbf{P}}^{(0)} = \Xi \left(\mathcal{A}_{\mathbf{1}}^* * \mathbf{Y}_1 \right) \\ \hat{\mathbf{Q}}^{(0)} = \Xi \left(\mathcal{A}_{\mathbf{2}}^* * \mathbf{Y}_2 \right), \end{cases}$$
(13)

where Ξ is the reshaping and concatenation operations, and the linear mapping in Eq. (3) is separately implemented using convolution operations with \mathcal{A}_1^* and \mathcal{A}_2^* . The final initial reconstruction $\hat{\mathbf{X}}^{(0)}$ is generated by applying the inverse DWT to the combination of $\hat{\mathbf{P}}^{(0)}$ and $\hat{\mathbf{Q}}^{(0)}$.

2) Deep Reconstruction: The deep reconstruction process is performed to the initial reconstruction result $\hat{\mathbf{X}}^{(0)}$ to improve its quality. By unfolding the iterative process in traditional MS-BCS reconstruction algorithm, we divide the module f_{deep} into Tstages. Each stage alternatively implements the projection (see Eq. (4)) in the wavelet domain and the full-image denoising (see (12)) in the spatial domain. At the (t + 1)-th stage, let $\hat{\mathbf{X}}^{(t)}$ be the reconstruction result of the previous stage. To perform the projection in (4) in the wavelet domain, we first decompose the image $\hat{\mathbf{X}}^{(t)}$ into sub-images $\hat{\mathbf{P}}^{(t)}$ and $\hat{\mathbf{Q}}^{(t)}$, in which $\hat{\mathbf{P}}^{(t)}$ represents the LL sub-band and $\hat{\mathbf{Q}}^{(t)}$ represents the stacking of the LH, HL and HH sub-bands. The projection operations for $\hat{\mathbf{P}}^{(t)}$ and $\hat{\mathbf{Q}}^{(t)}$ are expressed as

$$\begin{cases} \hat{\mathbf{P}}^{(t+1)} = \hat{\mathbf{P}}^{(t)} + \hat{\mathbf{P}}^{(0)} - \Xi \left(\mathcal{A}_{1}^{*} * \left(\left(\mathcal{A}_{1} * \hat{\mathbf{P}}^{(t)} \right) \odot \mathbf{M}_{\mathcal{A}_{1}} \right) \right) \\ \hat{\mathbf{Q}}^{(t+1)} = \hat{\mathbf{Q}}^{(t)} + \hat{\mathbf{Q}}^{(0)} - \Xi \left(\mathcal{A}_{2}^{*} * \left(\left(\mathcal{A}_{2} * \hat{\mathbf{Q}}^{(t)} \right) \odot \mathbf{M}_{\mathcal{A}_{2}} \right) \right). \end{cases}$$

By applying the IDWT on the combination of $\hat{\mathbf{P}}^{(t+1)}$ and $\hat{\mathbf{Q}}^{(t+1)}$, we can obtain the projection result $\hat{\mathbf{X}}^{(t+1)\prime}$ of the (t+1)-th stage.

For the full-image denoising operation in (12), we use the denoising block to remove the noise of $\hat{\mathbf{X}}^{(t+1)'}$ to get the (t+1)-th reconstruction result $\hat{\mathbf{X}}^{(t+1)}$. In each denoising block, the first (d-1) layers generate w feature maps using 3×3 convolution and the ReLU activation function, and the last layer generates a feature map using 3×3 convolution without activation function. The architecture of the denoising block is designed by removing the batch normalization layer between the convolutional layer and ReLU activation function in the feed-forward denoising model [27].

After finishing all the *T* stages, the final reconstructed image $\hat{\mathbf{X}}^{(T)}$ can be generated. Formally, let $\mathbb{S}_{\Theta} = \{\Theta_1, \Theta_2, \dots, \Theta_T\}$ represent the learnable weights of all the denoising blocks. Then the total process of the reconstruction model can be expressed

as

$$\hat{\mathbf{X}}^{(T)} = f_{rec} \left(\mathbf{Y}_1, \mathbf{Y}_2, \mathbb{S}_{\Theta}, \mathcal{A}_1, \mathcal{A}_1^*, \mathcal{A}_2, \mathcal{A}_2^* \right).$$
(15)

C. Loss Function

The forward propagation process of the AMS-Net is shown in Algorithm 2, where the whole model can be trained end-to-end and all the parameters are adaptively learned through backward propagation.

The mean squared error (MSE) is widely used as the loss function in many state-of-the-art deep learning-based CS methods [14], [15], [20], since it is differentiable and has faster convergence speed than other loss functions such as l_1 loss and perceptual loss [28]. To obtain the fastest convergence speed and best reconstruction performance, we also use MSE as the loss function to calculate the difference between the original image and its corresponding reconstructed image. Given N training images $\{\mathbf{X}_i\}_{i=1}^N$, the loss function is calculated by

$$\mathcal{L} = \frac{1}{2N} \sum_{i=1}^{N} \| f_{rec} \left(f_{samp} \left(\mathbf{X}_{i}, sr_{i}, \mathcal{A}_{1}, \mathcal{A}_{2} \right), \right. \\ \left. \mathbb{S}_{\Theta}, \mathcal{A}_{1}, \mathcal{A}_{2}, \mathcal{A}_{1}^{*}, \mathcal{A}_{2}^{*} \right) - \mathbf{X}_{i} \|_{2}^{2},$$
(16)

where sr_i is the target sampling ratio of the *i*-th original image X_i in the training set. Using this loss function, the AMS-Net can quickly minimize the error between the reconstructed image and the original image in the training process.

V. EXPERIMENTAL RESULTS AND PERFORMANCE EVALUATIONS

In this section, we first design the training method to evaluate the performance of the AMS-Net, and then compare it with state-of-the-art schemes in terms of reconstruction quality, visual effect, and model complexity.

A. Experiment Settings

The image block size in the sampling model is set as B = 16and the number of reconstruction stage T is set as 10. The width w and depth d of the denoising block in each reconstruction stage are set as 64 and 5, respectively. For the target sampling ratio srin the original image, the allocation ratio ar is set as ar = 0.95when $sr \le 0.05$, and set as $ar = \max(0.25, 0.95 - sr)$ when sr > 0.05. The parameter studies about the stage T, the width wand depth d, and the allocation ratio ar are shown in Section V-D.

1) Training: Our experiment uses the same database with other models [14], [16] to build the training dataset. Specifically, the training set is constructed using the training set (200 images) and testing set (200 images) of the BSD500 [29], [30], [31] dataset. We randomly flip and rotate these original images to extend our dataset, which is the same with the CSNet⁺ [14]. Then we randomly crop $400 \times 224 = 89600$ gray-scale sub-images of size 128×128 as the training set.

To speed up the training process and improve the reconstruction performance, we use a pre-trained denoising block to initialize the weights of all the denoising blocks in the proposed model. Specifically, following the settings in [27], we pretrain Algorithm 2: The forward propagation of the AMS-Net.

Input: $\mathbf{X}, sr, \mathcal{A}_1, \mathcal{A}_2, \mathcal{A}_1^*, \mathcal{A}_2^*, \mathbb{S}_{\Theta}, T$ Output: \hat{X}^{T} **procedure** Sampling($\mathbf{X}, sr, \mathcal{A}_1, \mathcal{A}_2$) 1: 2: $sr_p, sr_q = SR_Assign(sr)$ $\mathbf{P}, \mathbf{Q} = DWT(X)$ 3: 4: $\mathbf{M}_{\mathcal{A}_1} = LSRA(sr_p, \mathbf{P})$ 5: $\mathbf{M}_{\mathcal{A}_2} = LSRA(sr_q, \mathbf{Q})$ $\mathbf{Y}_1 = (\mathcal{A}_1 * \mathbf{P}) \odot \mathbf{M}_{\mathcal{A}_1}$ 6: $\mathbf{Y}_2 = (\mathcal{A}_2 * \mathbf{Q}) \odot \mathbf{M}_{\mathcal{A}_2}$ 7: 8: return $\mathbf{Y}_1, \mathbf{Y}_2$ 9: end procedure **procedure** Reconstruction($\mathbf{Y}_1, \mathbf{Y}_2, \mathcal{A}_1^*, \mathcal{A}_2^*, \mathbb{S}_{\Theta}, T$) 10: $\hat{\mathbf{P}}^{(0)} = \Xi(\mathcal{A}_1^* * \mathbf{Y}_1)$ 11: $\hat{\mathbf{Q}}^{(0)} = \Xi(\mathcal{A}_{2}^{*} * \mathbf{Y}_{2})$ $\hat{\mathbf{X}}^{(0)} = IDWT\left(\hat{\mathbf{P}}^{(0)}, \hat{\mathbf{Q}}^{(0)}\right)$ 12: 13: t = 014: while $(t+1) \leq T$ do \triangleright In the (t+1)th stage 15: $\hat{\mathbf{P}}^{(t)}, \hat{\mathbf{Q}}^{(t)} = DWT\left(\hat{\mathbf{X}}^{\mathbf{t}}\right)$ 16: $\hat{\mathbf{P}}^{(t+1)} = \\ \hat{\mathbf{P}}^{(t)} + \hat{\mathbf{P}}^{(0)} - \Xi \left(\mathcal{A}_{1}^{*} * \left(\left(\mathcal{A}_{1} * \hat{\mathbf{P}}^{(t)} \right) \odot \mathbf{M}_{\mathcal{A}_{1}} \right) \right)$ 17: $\hat{\mathbf{Q}}^{(t+1)} =$ 18: $\hat{\hat{\mathbf{Q}}}^{(t)} + \hat{\hat{\mathbf{Q}}}^{(0)} - \Xi \left(\mathcal{A}_{\mathbf{2}}^* * \left(\left(\mathcal{A}_{\mathbf{2}} * \hat{\mathbf{Q}}^{(t)} \right) \odot \mathbf{M}_{\mathcal{A}_{\mathbf{2}}} \right) \right)$ $\hat{\mathbf{X}}^{(t+1)\prime} = IDWT \left(\hat{\mathbf{P}}^{(t+1)}, \hat{\mathbf{Q}}^{(t+1)} \right)$ 19: $\hat{\mathbf{X}}^{(t+1)} = \hat{\mathbf{X}}^{(t+1)\prime} + \mathcal{D}\left(\hat{\mathbf{X}}^{(t+1)\prime}, \boldsymbol{\Theta}_{(t+1)}^{\prime}\right)$ 20: 21: t = t + 1end while 22: return $\hat{\mathbf{X}}^{(t)}$ 23: 24: end procedure

a single denoising block for blind Gaussian denoising task with random noise levels $\sigma \in [0, 55]$. The training epochs are 50 and the batch size is 64. The Adam optimization strategy [32] with a learning rate of 0.0001 is employed to optimize the parameters of the denoising block. Our AMS-Net is trained with batch size 1 for 10 epochs. For every mini-batch, a random sampling ratio within [0.01,0.50] is set for the used image. The optimizer is the Adam optimizer, and the learning rate decays linearly from 0.0001 to 0.00001 on these ten epochs. The TensorFlow framework is used to implement the proposed model, and all the experiments are implemented on a workstation with two GeForce RTX3090 GPUs and an Intel(R) Core(TM) i9-10920X CPU. It takes about one hour for one epoch in the training process.

2) Testing: Four widely used benchmark datasets, including the Set5 (5 images) [35], Set11 (11 images) [23], Set14 (14 images) [36], and the validating dataset of BSD500 called BSD100 (100 images), are used for evaluation. These widely used datasets contain different image features and can fairly reflect the reconstruction performance of different models. To keep consistency with the training process, we also convert all the color images in these four datasets into gray-scale images and use the obtained gray-scale images as the testing images.

 TABLE II

 PSNR AND SSIM COMPARISONS OF OUR AMS-NET WITH THE TRADITIONAL CS METHODS UNDER MULTIPLE SAMPLING RATIOS (sr)

	Set5 (PSNR/SSIM)								
sr Methods	0.01	0.03	0.05	0.1	0.2	0.3	0.4	0.5	Avg.
DAMP-R [33]	6.54/0.0491	12.08/0.2859	17.73/0.4424	23.24/0.6431	25.12/0.8092	31.65/0.8860	34.46/0.9197	30.97/0.9310	22.72/0.6208
DAMP-L [33]	10.97/0.2967	19.92/0.6062	24.20/0.7293	28.77/0.8426	32.44/0.9181	32.32/0.9413	36.23/0.9557	33.39/0.9605	27.28/0.7813
FOCUSS-R [13]	17.09/0.4531	20.27/0.5737	22.71/0.6439	25.86/0.7356	29.40/0.8267	31.62/0.8741	33.46/0.9045	35.12/0.9262	26.94/0.7422
FOCUSS-L [13]	21.88/0.5520	25.01/0.6863	26.89/0.7630	29.59/0.8481	32.87/0.9136	35.33/0.9429	37.47/0.9595	39.37/0.9699	31.05/0.8294
MH-R [34]	15.70/0.3936	21.21/0.5791	23.93/0.6726	27.44/0.7923	30.63/0.8686	32.60/0.9016	34.25/0.9245	35.77/0.9411	27.69/0.7592
MH-L [34]	19.12/0.5047	25.29/0.7142	27.30/0.7840	30.08/0.8656	33.28/0.9252	35.72/0.9508	37.86/0.9660	39.94/0.9759	31.07/0.8358
TV-R [11]	17.09/0.4135	18.81/0.4788	21.13/0.5550	24.63/0.6939	28.24/0.8182	30.83/0.8795	33.04/0.9172	35.11/0.9423	26.11/0.7123
TV-L [11]	21.40/0.5295	24.53/0.6862	26.34/0.7678	28.89/0.8531	31.65/0.9143	33.63/0.9419	35.45/0.9588	37.27/0.9704	29.89/0.8277
BCS-SPL-R [21]	17.50/0.4705	20.44/0.5744	22.58/0.6492	25.61/0.7376	29.00/0.8219	31.17/0.8675	33.00/0.8984	34.70/0.9212	26.75/0.7426
BCS-SPL-L [21]	22.20/0.5712	25.59/0.7126	27.53/0.7870	30.41/0.8685	33.71/0.9250	36.05/0.9502	38.14/0.9652	40.16/0.9750	31.72/0.8443
MS-BCS-R [12]	-/-	24.63/0.6613	26.27/0.7188	29.46/0.8372	32.65/0.8919	34.90/0.9402	36.15/0.9432	37.40/0.9491	-/-
AMS-Net-R	20.47/0.5529	24.71/0.7050	27.83/0.8013	31.61/0.8778	35.34/0.9314	37.69/0.9526	39.67/0.9643	41.51/0.9716	32.35/0.8446
AMS-Net	23.00/0.6261	27.97/0.7987	30.37/0.8563	33.41/0.9066	36.64/0.9445	39.01/0.9616	41.25/0.9722	43.28/0.9793	34.37/0.8807
				Set14 (PSNR	/SSIM)				
Methods	0.01	0.03	0.05	0.1	0.2	0.3	0.4	0.5	Avg.
DAMP-R [33]	6.14/0.0424	12.06/0.2656	17.49/0.3987	21.95/0.5557	25.65/0.6995	28.20/0.7800	30.63/0.8361	33.41/0.8813	21.94/0.5574
DAMP-L [33]	11.37/0.2864	18.92/0.5323	22.97/0.6463	26.20/0.7605	29.47/0.8535	31.77/0.8982	33.70/0.9244	35.53/0.9427	26.24/0.7305
FOCUSS-R [13]	17.89/0.4269	20.01/0.5073	21.48/0.5623	23.91/0.6534	26.76/0.7569	28.76/0.8191	30.46/0.8617	32.07/0.8942	25.17/0.6852
FOCUSS-L [13]	20.85/0.4847	23.30/0.5997	24.60/0.6685	26.73/0.7697	29.57/0.8638	31.82/0.9088	33.81/0.9350	35.69/0.9515	28.30/0.7727
MH-R [34]	16.26/0.3594	20.40/0.5074	22.33/0.5869	25.36/0.7011	28.28/0.8070	30.17/0.8572	31.74/0.8896	33.37/0.9169	25.99/0.7032
MH-L [34]	18.54/0.4402	23.49/0.6133	24.86/0.6803	27.04/0.7811	29.99/0.8737	32.14/0.9158	34.44/0.9426	36.38/0.9585	28.36/0.7757
TV-R [11]	17.22/0.3809	18.78/0.4363	20.46/0.4993	23.11/0.6173	26.15/0.7406	28.36/0.8137	30.38/0.8643	32.34/0.9020	24.60/0.6568
TV-L [11]	20.55/0.4738	23.12/0.5994	24.40/0.6681	26.43/0.7685	29.17/0.8599	31.14/0.9044	33.01/0.9321	34.89/0.9512	27.84/0.7697
BCS-SPL-R [21]	17.72/0.4347	19.77/0.5056	21.22/0.5598	23.67/0.6498	26.52/0.7494	28.55/0.8116	30.26/0.8558	31.91/0.8904	24.95/0.6821
BCS-SPL-L [21]	21.06/0.5003	23.66/0.6179	25.05/0.6875	27.30/0.7866	30.30/0.8744	32.47/0.9159	34.43/0.9408	36.39/0.9571	28.83/0.7850
MS-BCS-R [12]	-/-	22.97/0.5729	24.29/0.6343	26.55/0.7430	29.27/0.8274	31.25/0.8945	32.70/0.9064	34.04/0.9198	-/-
AMS-Net-R	19.89/0.4864	23.64/0.6117	25.73/0.6861	28.58/0.7795	32.08/0.8697	34.39/0.9122	36.21/0.9354	37.77/0.9490	29.79/0.7788
AMS-Net	22.20/0.5470	25.63/0.6720	27.38/0.7350	30.12/0.8182	33.34/0.8945	35.59/0.9298	37.54/0.9499	39.23/0.9619	31.38/0.8135

The competing methods contain six traditional CS methods, including the DAMP [33], BCS-FOCUSS [13], TV [11], MH [34], BCS-SPL [21] and MS-BCS [12], five single-scale deep learning-based CS models, including the ReconNet [23], ISTA-Net [37], CSNet⁺ [14], ISTA-Net⁺⁺ [38] and AMP-Net [15], and six multi-scale deep learning-based CS models, including the SCSNet [16], MSRNet [17], MS-DCSNet [18], DoC-DCS [19], P-DCI [20] and SS-DCI [20]. The reconstruction performance is tested by calculating the Peak Signalto-Noise Ratio (PSNR) [39] and Structural Similarity Index (SSIM) [40] between the reconstructed image and original image. A higher PSNR or SSIM score means the better reconstruction quality. Besides, the visual quality is also compared by showing the reconstruction results of different methods.

B. Comparison With Traditional CS Methods

First, we compare our AMS-Net with six traditional CS methods, DAMP [33], BCS-FOCUSS [13], TV [11], MH [34], BCS-SPL [21] and MS-BCS [12]. All codes of the traditional CS methods are directly downloaded from the authors' websites, and the default parameters are used for evaluation. Two kinds of measurement matrices are used, including the random measurement matrices (i.e. Gaussian matrices) and learned measurement matrices. The learned measurement matrices are generated as follows. First, two convolutional layers are used to sample the image and recover the initial reconstruction results from the sampled measurements, respectively. Then, using these

two learnable layers, we construct a small model and train it using the training set. By converting the learned weights of the sampling layer into matrix, we can get the learned measurement matrices.

1) Reconstruction Quality: Table II shows the comparison results of our AMS-Net with traditional CS methods on Set5 and Set14, respectively. For traditional CS methods, the suffix '-R' denotes that the measurement matrices are randomly generated while the suffix '-L' means that the measurement matrices are learned. For our AMS-Net, the suffix '-R' means that the measurement matrices are non-learnable in the training process. The sampling ratio varies from 0.01 to 0.5. Note that the MS-BCS [12] cannot work at a sampling ratio lower than 0.02 and it samples image in the multi-level wavelet domain with different block sizes. Thus, its measurement matrices are difficult to learn. We only test it with random measurement matrices and do not provide the test result at sampling ratio 0.01 for MS-BCS.

As can be see from Table II, when using the learned measurement matrices to replace the random measurement matrices, the reconstruction performance of all the traditional CS methods can be greatly improved, and the average PSNR scores are improved about $3 \sim 5$ dB for every traditional CS methods. Meanwhile, using the learned measurement matrices, the average PSNR scores of our AMS-Net can be improved about $2 \sim 3$ dB than using the random measurement matrices. Thus, it is obvious that the learned measurement matrices are much more effective than these randomly generated measurement matrices. From Table II, we can see that the PSNR and SSIM scores of our AMS-Net are significantly larger than those of the traditional methods. Thus,

FOCUSS-R [13] FOCUSS-L [13] Original image DAMP-R [33] DAMP-L [33] MH-R [34] MH-L [34] 13.74/0.3487 PSNR/SSIM 19.23/0.6651 17.52/0.5135 20.90/0.6646 17.64/0.5333 21.01/0.6906 TV-R [11] TV-L [11] BCS-SPL-R [21] BCS-SPL-L [21] MS-BCS-R [12] AMS-Net-R AMS-Net 15.95/0.4528 21.25/0.7556 17.25/0.5163 21.45/0.7028 19.91/0.5912 22.25/0.7795 26.02/0.8704

Fig. 5. Reconstructed results of image "butterfly" by our AMS-Net and the traditional CS methods under sampling ratio 0.05.

our AMS-Net can outperform all the traditional CS methods under all the sampling ratios. For example, in the comparison on Set5, when the traditional CS methods use random measurement matrices, the average PSNR score of the AMS-Net is 11.65 dB, 7.43 dB, 6.68 dB, 8.26 dB, 7.62 dB larger than the PSNR scores of the DAMP [33], BCS-FOCUSS [13], MH [34], TV [11], and BCS-SPL [21], respectively, while the corresponding average SSIM score is 0.2599, 0.1385, 0.1215, 0.1684 and 0.1261 larger than these methods, respectively. Besides, when using the random measurement matrices, our AMS-Net still outperforms all other traditional CS methods.

2) Visual Effect: To show the high reconstruction performance of our model, we compare the visual quality of our model with the traditional CS methods using the image "butterfly" from Set5. The comparison results are shown in Fig. 5, where the used sampling ratio is 0.05. As can be seen, there is obvious blocking artifacts in the reconstructed images by the traditional CS methods. However, our model can eliminate these blocking artifacts. This is because the denoising and deblocking modules in our model are learnable, and they can produce better denoising and deblocking performance than the traditional denoising methods. Meanwhile, by comparing the two versions of traditional CS methods, we can find that all the traditional CS methods can obtain better visual quality when using the learned measurement matrices. This visual quality results further verify the high performance of the measurement matrix learning strategy.

C. Comparison With Deep Learning-Based CS Methods

These competing deep learning-based methods, including the ReconNet [23], ISTA-Net [37], CSNet⁺ [14], ISTA-Net⁺⁺ [38], AMP-Net [15], SCSNet [16], MSRNet [17], DoC-DCS [19],

P-DCI [20], SS-DCI [20], MS-DCSNet [18], are all developed recently with high performance. For the ReconNet [23], ISTA-Net [37], CSNet⁺ [14], SCSNet [16], MSRNet [17], DoC-DCS [19], P-DCI [20], SS-DCI [20] and MS-DCSNet [18], we re-train them using the training set strictly following the details in the original literature. For the ISTA-Net⁺⁺ [38] and AMP-Net [15], we download their pre-trained models from the authors' websites and run these models on the testing datasets to get the results.

1) Reconstruction Quality: Table III shows the comparison results of different networks on the four testing datasets. As can be seen, the AMS-Net can obtain significantly higher PSNR scores than these deep learning-based CS methods over all sampling ratios and achieve larger SSIM scores in most cases. For example, the average PSNR score of the AMS-Net on Set11 is 2.12 dB, 4.24 dB, 7.06 dB, 2.11 dB, 4.9 dB, 1.47 dB, 2.11 dB, 4.78 dB, 1.80 dB, 2.26 dB, 1.75 dB and 2.14 dB larger than the PSNR scores of the CSNet⁺ [14], ISTA-Net [37], ReconNet [23], AMP-Net [15], ISTA-Net⁺⁺ [38], SCSNet [16], MSRNet [17], DoC-DCS [19], P-DCI [20], SS-DCI [20] and MS-DCSNet [18], respectively, while the corresponding average SSIM score on Set11 is 0.0160, 0.0789, 0.1376, 0.0088, 0.1114, 0.0148, 0.0689, 0.0098, 0.0142, 0.0081, 0.0148 larger than these methods, respectively.

Note that the SSIM score is calculated by a sliding Gaussian window in the spatial domain. However, our proposed model performs the sampling and projection operations in the wavelet domain, and this may slightly affect the SSIM scores of our method. Although our model gets a little smaller SSIM scores than the AMP-Net [15] under some sampling ratios, it can obtain the best SSIM score on average among all the methods. This indicates that our model can get the best reconstruction

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 TABLE III

 PSNR AND SSIM COMPARISONS OF OUR AMS-NET WITH THE DEEP LEARNING-BASED CS METHODS UNDER MULTIPLE SAMPLING RATIOS (sr)

	Set5 (PSNR/SSIM)								
sr	0.01	0.03	0.05	0.1	0.2	0.3	0.4	0.5	4
Methods	0.01	0.05	0.05	0.1	0.2	0.5	0.4	0.5	Avg.
CSNet ⁺ [14]	22.78/0.6094	26.49/0.7665	28.60/0.8316	31.54/0.8956	34.86/0.9396	36.95/0.9581	38.67/0.9692	40.63/0.9774	32.56/0.8684
ISTA-Net [37]	19.32/0.4669	22.61/0.6138	24.82/0.7130	28.31/0.8272	32.56/0.9083	35.17/0.9400	37.24/0.9574	39.31/0.9701	29.92/0.7996
ReconNet [23]	18.44/0.4660	21.91/0.5863	23.57/0.6409	26.06/0.7332	28.97/0.8185	31.25/0.8738	32.71/0.8956	34.46/0.9226	27.17/0.7421
AMP-Net [15]	22.42/0.6183	26.56/0.7789	28.62/0.8380	32.10/0.9024	35.55/0.9427	37.87/0.9608	39.77/0.9717	41.60/ 0.9793	33.06/0.8740
ISTA-Net ⁺⁺ [38]	12.60/0.3081	16.67/0.4658	25.41/0.7539	30.22/0.8702	33.94/0.9250	36.27/0.9485	38.13/0.9621	39.95/0.9725	29.15/0.7758
SCSNet [16]	22.78/0.6136	26.47/0.7654	28.69/0.8331	31.58/0.8968	34.86/0.9404	36.87/0.9586	38.80/0.9701	40.81/0.9786	32.61/0.8696
MSRNet [17]	22.06/0.5723	25.17/0.7019	27.34/0.7888	29.03/0.8265	32.07/0.8946	33.58/0.9117	33.89/0.9114	34.85/0.9239	29.75/0.8164
P-DCI [20]	22.72/ 0.6280	26.21/0.7719	28.51/0.8320	31.47/0.8942	34.62/0.9375	36.49/0.9541	38.13/0.9638	39.78/0.9732	32.24/0.8693
SS-DCI [20]	22.05/0.6054	26.67/0.7864	29.02/0.8456	31.89/0.9017	35.00/0.9407	37.38/0.9604	39.01/0.9699	40.99/0.9781	32.75/0.8735
MS-DCSNet [18]	22.70/0.6218	26.37/0.7691	28.33/0.8297	31.19/0.8928	34.62/0.9344	36.75/0.9540	38.40/0.9648	40.29/0.9741	32.33/0.8676
DoC-DCS [19]	22.06/0.5995	26.63/0.7870	28.90/0.8457	31.98/0.9016	34.94/0.9419	37.38/0.9600	39.05/0.9701	40.72/0.9768	32.71/0.8728
AMS-Net	23.00 /0.6261	27.97/0.7987	30.37/0.8563	33.41/0.9066	36.64/0.9445	39.01/0.9616	41.25/0.9722	43.28/0.9793	34.37/0.8807
				Set14 (PSNR	/SSIM)				
sr	0.01	0.03	0.05	0.1	0.2	0.3	0.4	0.5	Ava
Methods	0.01	0.05	0.05	0.1	0.2	0.5	0.4	0.5	Avg.
CSNet ⁺ [14]	21.59/0.5309	24.30/0.6477	25.71/0.7125	27.96/0.8028	31.01/0.8846	33.14/0.9232	35.01/0.9454	36.97/0.9606	29.46/0.8010
ISTA-Net [37]	18.56/0.4122	21.24/0.5293	23.07/0.6122	25.74/0.7237	29.19/0.8354	31.70/0.8913	33.90/0.9246	35.99/0.9479	27.43/0.7346
ReconNet [23]	18.01/0.4175	20.65/0.5056	22.03/0.5586	24.02/0.6419	26.40/0.7404	28.43/0.8123	29.79/0.8494	31.47/0.8869	25.10/0.6766
AMP-Net [15]	21.65/0.5435	24.62/0.6629	26.13/0.7267	28.77/ 0.8182	32.00/0.8938	34.38/ 0.9301	36.34/ 0.9512	38.22/ 0.9650	30.26/0.8114
ISTA-Net ⁺⁺ [38]	12.32/0.2506	16.09/0.3863	23.35/0.6445	27.32/0.7714	30.72/0.8628	33.07/0.9074	34.98/0.9341	36.73/0.9525	26.82/0.7137
SCSNet [16]	21.61/0.5323	24.31/0.6478	25.79/0.7139	27.99/0.8041	30.98/0.8855	33.15/0.9239	35.08/0.9466	37.08/0.9619	29.50/0.8020
MSRNet [17]	21.10/0.5026	23.47/0.6074	24.98/0.6822	26.31/0.7388	28.93/0.8415	30.41/0.8726	30.80/0.8783	31.66/0.8934	27.21/0.7521
P-DCI [20]	21.65/0.5411	24.06/0.6494	25.67/0.7114	28.05/0.8031	30.87/0.8842	32.85/0.9189	34.55/0.9395	35.68/0.9492	29.17/0.7996
SS-DCI [20]	21.22/0.5251	24.45/0.6641	25.98/0.7264	28.27/0.8143	31.18/0.8896	33.55/0.9278	35.27/0.9464	37.42/0.9625	29.67/0.8070
MS-DCSNet [18]	21.57/0.5396	24.20/0.6470	25.71/0.7123	27.86/0.8011	30.98/0.8818	33.04/0.9188	34.96/0.9432	36.73/0.9563	29.38/0.8000
DoC-DCS [19]	21.29/0.5204	24.43/0.6651	25.93/0.7264	28.34/0.8153	31.12/0.8909	33.40/0.9265	35.31/0.9474	37.08/0.9592	29.61/0.8064
AMS-Net	22.20/0.5470	25.63/0.6720	27.38/0.7350	30.12/0.8182	33.34/0.8945	35.59 /0.9298	37.54 /0.9499	39.23 /0.9619	31.38/0.8135
				Set11 (PSNR	/SSIM)				
sr	0.01	0.03	0.05	0.1	0.2	0.3	0.4	0.5	Avia
Methods	0.01	0.05	0.05	0.1	0.2	0.5	0.4	0.5	Avg.
							26 70 10 0655		
CSNet ⁺ [14]	21.06/0.5588	24.13/0.7169	26.06/0.7913	28.66/0.8644	32.10/0.9219	34.65/0.9509	36.78/0.9655	38.93/0.9763	30.30/0.8433
CSNet ⁺ [14] ISTA-Net [37]	21.06/0.5588 18.16/0.4394	24.13/0.7169 20.83/0.5731	26.06/0.7913 22.90/0.6746	28.66/0.8644 26.32/0.8010	32.10/0.9219 30.55/0.8973	34.65/0.9509 33.33/0.9343	36.78/0.9655 35.63/0.9549	38.93/0.9763 37.72/0.9687	30.30/0.8433 28.18/0.7804
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23]	21.06/0.5588 18.16/0.4394 17.44/0.4417	24.13/0.7169 20.83/0.5731 20.20/0.5446	26.06/0.7913 22.90/0.6746 21.66/0.6081	28.66/0.8644 26.32/0.8010 24.03/0.7076	32.10/0.9219 30.55/0.8973 26.88/0.8023	34.65/0.9509 33.33/0.9343 29.23/0.8631	36.78/0.9655 35.63/0.9549 30.83/0.8892	38.93/0.9763 37.72/0.9687 32.58/0.9172	30.30/0.8433 28.18/0.7804 25.36/0.7217
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586	36.78/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/ 0.9804	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478	36.78/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/ 0.9804 38.73/0.9727	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511	36.7870.9655 35.6370.9549 30.8370.8892 38.2870.9715 36.9470.9628 36.8170.9663	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/ 0.9804 38.73/0.9727 39.04/0.9775	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974	36.7870.9655 35.6370.9549 30.8370.8892 38.2870.9715 36.9470.9628 36.8170.9663 31.6270.8975	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/ 0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482	36.78/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/ 0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560	36.78/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/ 0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566 21.30/0.5734	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/ 0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.28/0.8445
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5764 21.30/0.5734 20.86/0.5734	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539	36.78/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/ 0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566 21.30/0.5734 20.86/0.5735	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7118 24.5/0.7418	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495 32.42/0.8593
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566 21.30/0.5734 20.86/0.5475 21.65/0.5795	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 29.04/0.8741 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM)	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8451 30.28/0.8445 30.62/0.8495 32.42/0.8593
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net sr	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566 21.30/0.5734 20.86/0.5475 21.65/0.5795	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.8041 27.91/0.8181	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM)	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599	36.78/0.9655 35.63/0.9549 30.83/0.8892 38.28/0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495 32.42/0.8593
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566 21.30/0.5734 20.86/0.5475 21.65/0.5795	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7412 25.69/0.7426 0.03	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2	34.65/0.9509 33.33/0.9543 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599	36.78/0.9655 35.63/0.9549 30.83/0.8892 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9685 37.31/0.9685 39.37/0.9702 0.4	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8451 30.28/0.8445 30.28/0.8445 32.42/0.8593 Avg.
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net Sr Methods CSNet ⁺ [14]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566 21.30/0.5734 20.86/0.5475 21.65/0.5795 0.01 22.47/0.5150	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.55/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.25/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111	36. /8/0.9655 35.63/0.9549 30.83/0.8892 36.94/0.9628 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702 0.4 33.68/0.9405	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 0.5 35.59/0.9604	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net Sr Methods CSNet ⁺ [14] ISTA-Net [37]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5747 20.86/0.5475 21.65/0.5795 0.01 22.47/0.5150 19.80/0.4215	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.03/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111 29.95/0.8656	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702 0.4 33.68/0.9405 31.82/0.9070	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 0 .5 35.59/0.9604 33.68/0.9367	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.62/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net <i>sr</i> Methods CSNet ⁺ [14] ISTA-Net [37] ReconNet [23]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5747 20.86/0.5475 21.36/0.5775 0.01 22.47/0.5150 19.80/0.4215 19.07/0.4242	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.5452	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8654 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.03/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.91111 29.95/0.8656 27.79/0.7931	36.78/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 0.5 35.59/0.9604 33.68/0.9367 30.66/0.8784	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.62/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net Sr Methods CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5747 20.86/0.5745 21.65/0.5795 0.01 22.47/0.5150 19.80/0.4215 19.07/0.4242 22.29/0.5231	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990 24.46/0.6231	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.5452 25.54/0.6840	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201 27.62/0.7787	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155 30.34/0.8702	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.91111 29.95/0.8656 27.79/0.7931 32.56/ 0.9178	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350 34.58/ 0.9466	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 5 .59/0.9604 33.68/0.9367 30.66/0.8784 36.57/ 0.9653	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638 29.25/0.7886
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net Sr Methods CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5747 20.86/0.5745 21.65/0.5795 0.01 22.47/0.5150 19.80/0.4215 19.07/0.4242 22.29/0.5231 13.38/0.2868	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990 24.46/0.6231 17.14/0.4134	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.5452 25.54/0.6840 23.22/0.6103	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201 27.62/0.7787 26.16/0.7265	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155 30.34/0.8702 28.85/0.8305	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111 29.95/0.8656 27.79/0.7931 32.56/ 0.9178 30.93/0.8869	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350 34.58/ 0.9466 32.81/0.9227	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 0 .5 35.59/0.9604 33.68/0.9367 30.66/0.8784 36.57/ 0.9653 34.64/0.9472	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638 29.25/0.7886 25.89/0.7030
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5747 21.30/0.5734 20.86/0.5475 21.65/0.5795 0.01 22.47/0.5150 19.80/0.4215 19.07/0.4242 22.29/0.5231 13.38/0.2868 22.47/0.5159	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990 24.46/0.6231 17.14/0.4134 24.37/0.6116	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.5452 25.54/0.6840 23.22/0.6103 25.48/0.6753	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201 27.62/0.7787 26.16/0.7265 27.26/0.7688	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155 30.34/0.8702 28.85/0.8305 29.76/0.8630	34.65/0.9509 33.33/0.9543 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111 29.95/0.8656 27.79/0.7931 32.56/0.9178 30.93/0.8869 31.78/0.9118	36.78/0.9655 35.63/0.9549 30.83/0.8892 38.28/0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37/0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350 34.58/0.9466 32.81/0.9227 33.70/0.9418	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 0 .5 35.59/0.9604 33.68/0.9367 30.66/0.8784 36.57/ 0.9653 34.64/0.9472 35.69/0.9621	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638 29.25/0.7886 25.89/0.7030 28.81/0.7813
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net SCSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566 21.30/0.5734 20.86/0.5475 21.65/0.5795 0.01 22.47/0.5150 19.80/0.4215 19.07/0.4242 22.29/0.5231 13.38/0.2868 22.47/0.5159 22.22/0.4992	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990 24.46/0.6231 17.14/0.4134 24.37/0.6116 23.89/0.5858	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.6840 23.22/0.6103 25.48/0.6753 25.03/0.6538	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201 27.62/0.7787 26.16/0.7265 27.26/0.7688 26.12/0.7148	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155 30.34/0.8702 28.85/0.8305 29.76/0.8630 28.29/0.8225	34.65/0.9509 33.33/0.9543 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111 29.95/0.8656 27.79/0.7931 32.56/ 0.9178 30.93/0.8869 31.78/0.9118 29.64/0.8609	36.78/0.9655 35.63/0.9549 30.83/0.8892 36.94/0.9628 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9685 39.37/0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350 34.58/0.9466 32.81/0.9227 33.70/0.9418 30.09/0.8696	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 0.5 35.59/0.9604 33.68/0.9367 30.66/0.8784 36.57/ 0.9653 34.64/0.9472 35.69/0.9621 31.04/0.8914	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638 29.25/0.7886 25.89/0.7030 28.81/0.7813 27.04/0.7373
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net <i>ST</i> Methods <i>CSNet</i> ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5566 21.30/0.5764 21.30/0.5764 21.30/0.5764 21.30/0.5765 21.65/0.5795 21.65/0.5795 21.65/0.5795 22.47 /0.5150 19.07/0.4242 22.29/0.5231 13.38/0.2868 22.47/0.5159 22.22/0.4992 22.58/0.5205	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990 24.48/0.4990 24.48/0.6231 17.14/0.4134 24.37/0.6116 23.89/0.5858 24.42/0.6174	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.5452 25.54/0.6840 23.22/0.6103 25.48/0.6753 25.03/0.6538 25.43/0.6745	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201 27.62/0.7787 26.16/0.7265 27.26/0.7688 26.12/0.7148 27.27/0.7679	32.10/0.9219 30.55/0.8973 32.688/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R /SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155 30.34/0.8702 28.85/0.8305 29.76/0.8630 28.29/0.8225 29.71/0.8627	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111 29.95/0.8656 27.79/0.7931 32.56/ 0.9178 30.93/0.8869 31.78/0.9118 29.64/0.8609 31.55/0.9070	36. /8/0.9655 35.63/0.9549 30.83/0.8892 36.94/0.9628 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9685 39.37/0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350 34.58/0.9466 32.81/0.9227 33.70/0.9418 30.09/0.8696 33.29/0.9356	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 41.05 /0.9770 35.59/0.9604 33.68/0.9367 30.66/0.8784 36.57/ 0.9653 34.64/0.9472 35.69/0.9621 31.04/0.8914 34.68/0.9509	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638 29.25/0.7886 25.89/0.7030 28.81/0.7813 27.04/0.7373 28.62/0.7795
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5747 20.86/0.5747 20.86/0.5745 21.65/0.5795 0.01 22.47/0.5150 19.80/0.4215 19.07/0.4242 22.29/0.5231 13.38/0.2868 22.47/0.5159 22.22/0.4992 22.58/0.5205 22.30/0.5095	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990 24.46/0.6231 17.14/0.4134 24.37/0.6116 23.89/0.5858 24.42/0.6174 24.56/0.6263	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.5452 25.54/0.6840 23.22/0.6103 25.48/0.6753 25.03/0.6538 25.43/0.6745 25.65/0.6868	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8674 29.04/0.8741 28.58/0.8648 29.04/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201 27.62/0.7787 26.16/0.7265 27.26/0.7688 26.12/0.7148 27.27/0.7679 27.48/0.7790	32.10/0.9219 30.55/0.8973 32.688/0.8023 33.21/0.9334 32.03/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155 30.34/0.8702 28.85/0.8305 29.76/0.8630 28.29/0.8225 29.71/0.8657 29.91/0.865	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111 29.95/0.8656 27.79/0.7931 32.56/ 0.9178 30.93/0.8869 31.78/0.9118 29.54/0.8609 31.55/0.9070 32.13/0.9175	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350 34.58/ 0.9466 32.81/0.9227 33.70/0.9418 30.09/0.8696 33.29/0.9356 33.93/0.9441	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 41.05 /0.9770 55 /0.9604 33.68/0.9367 30.66/0.8784 36.57/0.9653 34.64/0.9472 35.69/0.9621 31.04/0.8914 34.68/0.9509 35.94/0.9638	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638 29.25/0.7886 25.89/0.7030 28.81/0.7813 27.04/0.7373 28.62/0.7795 28.99/0.7867
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net MS-Net CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5747 20.86/0.5747 20.86/0.5475 21.30/0.5747 20.86/0.5475 21.65/0.5795 22.47/0.5150 19.80/0.4215 19.07/0.4242 22.29/0.5231 13.38/0.2868 22.47/0.5159 22.22/0.4992 22.58/0.5205 22.30/0.5095 22.30/0.5055	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990 24.46/0.6231 17.14/0.4134 24.37/0.6116	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.5452 25.54/0.6840 23.22/0.6103 25.48/0.6753 25.03/0.6538 25.43/0.6745 25.65/0.6868 25.45/0.6750	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8654 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201 27.62/0.7787 26.16/0.7265 27.26/0.7688 26.12/0.7148 27.27/0.7679 27.48/0.7790 27.16/0.7662	32.10/0.9219 30.55/0.8973 32.688/0.8023 33.21/0.9334 32.03/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155 30.34/0.8702 28.85/0.8305 29.76/0.8630 28.29/0.8225 29.71/0.8627 29.91/0.8665 29.75/0.8600	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111 29.95/0.8656 27.79/0.7931 32.56/ 0.9178 30.93/0.8869 31.78/0.9118 29.64/0.8609 31.55/0.9070 32.13/0.9175 31.78/0.9097	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350 34.58/ 0.9466 32.81/0.9227 33.70/0.9418 30.09/0.8696 33.29/0.9356 33.93/0.9441 33.64/0.9392	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 41.05 /0.9770 5 .59/0.9604 33.68/0.9367 30.66/0.8784 36.57/ 0.9653 34.64/0.9472 35.69/0.9621 31.04/0.8914 31.04/0.8914 35.57/0.9595	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.62/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638 29.25/0.7886 25.89/0.7030 28.81/0.7813 27.04/0.7373 28.62/0.7795 28.99/0.7867 28.79/0.7808
CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] SS-DCI [20] MS-DCSNet [18] DoC-DCS [19] AMS-Net CSNet ⁺ [14] ISTA-Net [37] ReconNet [23] AMP-Net [15] ISTA-Net ⁺⁺⁺ [38] SCSNet [16] MSRNet [17] P-DCI [20] MS-DCSNet [18] DoC-DCS [19]	21.06/0.5588 18.16/0.4394 17.44/0.4417 20.20/0.5581 11.30/0.2375 21.11/0.5616 20.66/0.5287 21.36/0.5747 20.86/0.5747 20.86/0.5747 20.86/0.5475 21.65/0.5745 21.65/0.5745 21.65/0.5745 19.07/0.4242 22.29/0.5231 13.38/0.2868 22.47/0.5159 22.22/0.4992 22.58/0.5205 22.30/0.5095 22.56/0.5205 22.24/0.5035	24.13/0.7169 20.83/0.5731 20.20/0.5446 24.11/0.7252 14.81/0.3832 24.13/0.7166 23.15/0.6572 24.04/0.7204 24.50/0.7411 24.15/0.7188 24.54/0.7422 25.69/0.7426 0.03 24.37/0.6123 21.86/0.5133 21.48/0.4990 24.46/0.6231 17.14/0.4134 24.37/0.6116 23.89/0.5858 24.42/0.6174 24.56/0.6263 24.41/0.6161 24.58/0.6270	26.06/0.7913 22.90/0.6746 21.66/0.6081 26.06/0.7987 22.88/0.7048 26.10/0.7939 25.12/0.7496 26.01/0.7931 26.50/0.8079 26.05/0.7927 26.31/0.8041 27.91/0.8181 0.05 25.45/0.6742 23.17/0.5825 22.55/0.5452 25.54/0.6840 23.22/0.6103 25.48/0.6753 25.03/0.6538 25.43/0.6745 25.65/0.6868	28.66/0.8644 26.32/0.8010 24.03/0.7076 29.40/0.8779 28.34/0.8531 28.66/0.8659 26.71/0.7984 28.88/0.8654 29.04/0.8741 28.58/0.8648 29.19/0.8753 31.23/0.8867 BSD100 (PSN 0.1 27.25/0.7671 25.14/0.6861 24.06/0.6201 27.62/0.7787 26.16/0.7265 27.26/0.7688 26.12/0.7148 27.27/0.7679 27.48/0.7790 27.48/0.7790	32.10/0.9219 30.55/0.8973 26.88/0.8023 33.21/0.9334 32.33/0.9217 32.02/0.9232 29.67/0.8746 32.15/0.9242 32.38/0.9268 32.20/0.9215 32.25/0.9273 34.99/0.9406 R/SSIM) 0.2 29.75/0.8615 27.87/0.8013 26.00/0.7155 30.34/0.8702 28.85/0.8305 29.76/0.8630 28.29/0.8225 29.71/0.8627 29.91/0.8665 29.75/0.8600 29.92/0.8689	34.65/0.9509 33.33/0.9343 29.23/0.8631 36.03/0.9586 34.86/0.9478 34.63/0.9511 31.29/0.8974 34.44/0.9482 35.30/0.9560 34.63/0.9478 35.26/0.9539 37.46/0.9599 0.3 31.81/0.9111 29.95/0.8656 27.79/0.7931 32.56/0.9178 30.93/0.8869 31.78/0.9118 29.64/0.8609 31.55/0.9070 32.13/0.9175 31.78/0.9097 31.95/0.9147	36. /8/0.9655 35.63/0.9549 30.83/0.8892 38.28/ 0.9715 36.94/0.9628 36.81/0.9663 31.62/0.8975 36.28/0.9615 37.30/0.9687 36.65/0.9627 37.31/0.9685 39.37 /0.9702 0.4 33.68/0.9405 31.82/0.9070 29.06/0.8350 34.58/ 0.9466 32.81/0.9227 33.70/0.9418 30.09/0.8696 33.93/0.9441 33.64/0.9392 33.93/0.9441	38.93/0.9763 37.72/0.9687 32.58/0.9172 40.33/0.9804 38.73/0.9727 39.04/0.9775 32.93/0.9197 38.11/0.9713 39.46/0.9787 38.68/0.9740 39.20/0.9770 41.05 /0.9770 41.05 /0.9770 55.59/0.9604 33.68/0.9367 30.66/0.8784 36.57/ 0.9653 34.64/0.9472 35.69/0.9621 31.04/0.8914 34.68/0.9509 35.94/0.9638 35.57/0.9595 35.78/0.9623	30.30/0.8433 28.18/0.7804 25.36/0.7217 30.95/0.8505 27.52/0.7479 30.31/0.8445 27.64/0.7904 30.16/0.8451 30.67/0.8512 30.28/0.8445 30.62/0.8495 32.42/0.8593 Avg. 28.80/0.7803 26.66/0.7143 25.08/0.6638 29.25/0.7886 25.89/0.7030 28.81/0.7813 27.04/0.7373 28.62/0.7795 28.99/0.7867 28.99/0.7808 28.94/0.7857

quality. Besides, compared with AMP-Net [15], our AMS-Net has some other important advantages. First, it can achieve much larger PSNR and SSIM scores when the sampling ratio is very low, which indicates that it shows much better performance in heavy compression tasks (see Fig. 6 and Table III). Second, our AMS-Net is a scalable method while AMP-Net [15] is not. This indicates that our method can sample images at arbitrary sampling ratios with only one-time training. However, a

single AMP-Net [15] model can sample images only at a fixed sampling ratio. Thus, to perform tasks with n sampling ratios, the AMP-Net [15] should train n models and thus has much more parameters than our AMS-Net, as shown in Table VII.

2) Visual Effect: We use the image "Parrots" in Set11 dataset to show the visual quality of the reconstructed images by different deep learning-based CS methods and Fig. 6 shows the reconstruction results under the sampling ratio 0.05. As



Fig. 6. Reconstructed results of image "Parrots" by our AMS-Net and the deep learning-based CS methods under sampling ratio 0.05.

TABLE IV

The Influence of the Number of Denoising Stages T, the Width w and Depth d of the Denoising Block, the LSRA Strategy L, and the Projection Operation P on the Average Reconstruction PSNR (dB) Performance on Set11 of Our Proposed AMS-Net

T	I D		T	Sampling Ratio ($w = 32/w = 64$)								A
L Γ	Р	a	1	0.01	0.03	0.05	0.1	0.2	0.3	0.4	0.5	Avg.
\checkmark	\checkmark	5	4	21.18/21.36	25.04/25.21	27.24/27.50	30.42/30.69	34.18/34.48	36.74/37.06	38.68/39.02	40.26/40.66	31.72/32.00
\checkmark	\checkmark	5	6	21.36/21.50	25.26/25.51	27.50/27.75	30.80/31.02	34.52/34.79	37.03/37.29	38.96/39.24	40.59/40.90	32.00/32.25
\checkmark	\checkmark	5	8	21.48/21.56	25.47/25.52	27.69/27.83	30.95/31.17	34.67/34.94	37.18/37.43	39.12/39.37	40.79/41.03	32.17/32.36
\checkmark	\checkmark	5	10	21.55/21.65	25.47/25.69	27.77/27.91	31.00/31.23	34.75/34.99	37.24/37.46	39.18/39.37	40.86/41.05	32.22/32.42
\checkmark	\checkmark	5	12	21.51/21.64	25.48/25.70	27.78/28.00	30.98/31.22	34.70/34.99	37.21/37.42	39.15/39.29	40.84/40.87	32.21/32.39
\checkmark	\checkmark	3	10	21.27/21.34	25.10/25.23	27.25/27.44	30.50/30.67	34.29/34.47	36.83/37.05	38.86/39.09	40.55/40.83	31.83/32.01
\checkmark	\checkmark	7	10	21.61/21.83	25.69/25.91	27.92/28.17	31.08/31.37	34.84/35.19	37.33/37.60	39.27/39.53	40.92/41.20	32.33/32.60
\checkmark	\checkmark	9	10	21.73/21.84	25.78/25.98	28.05/28.27	31.27/31.44	35.01/35.23	37.51/37.64	39.44/39.60	41.10/41.30	32.49/32.66
\checkmark	\checkmark	11	10	21.79/21.88	25.84/26.03	28.12/28.26	31.27/31.43	35.01/35.27	37.47/37.66	39.38/39.60	41.05/41.28	32.49/32.68
	\checkmark	5	10	21.00/21.15	24.50/24.62	26.65/26.75	29.69/29.87	33.38/33.60	36.00/36.23	37.20/36.84	38.28/37.93	30.84/30.87
\checkmark		5	10	20.65/20.79	24.11/24.33	26.07/26.39	28.85/29.12	31.99/32.30	34.42/34.71	36.28/36.57	37.50/37.84	29.98/30.26

can be seen, the reconstructed images by the ReconNet [23], ISTA-Net [37], ISTA-Net⁺⁺ [38] and MSRNet [17] have obvious blocking artifacts. This is because these methods focus on the reconstruction of each image block individually, and don't consider the correlations between adjacent blocks. On the contrary, there aren't obvious blocking artifacts in the reconstructed images generated by other models, because these models all apply denoising and deblocking operations to the full-image on the reconstruction stage. As shown in Fig. 6, the image reconstructed by our AMS-Net contains more details and sharp edges of the original image than the images reconstructed by other methods. Thus, compared with other methods, our AMS-Net has stronger ability to remove blocking artifacts and reconstruct images with higher visual quality.

D. Discussion

In this section, we evaluate the influence of model parameters and model structure on the reconstruction performance of our AMS-Net. 1) Depth and Width of the Denoising Block: The number of parameters in our AMS-Net is influenced by the width w and depth d of the denoising block. Here, we investigate the parameter capacity by setting w as 32 and 64, and setting d ranging from 3 to 11. As can be seen from Table IV, when fixing d and changing w from 32 to 64, the average PSNR scores can be improved about 0.2 dB. Besides, the reconstruction quality gradually rises until d grows to 9. When d > 9, the model appears to be over-fitting and slightly declines in the reconstruction performance. Thus, to achieve a relatively high reconstruction quality and small parameter capacity, we set w = 64 and d = 5 in our model.

2) Projection Operation: By utilizing the projection operation, our model can integrate the structure advantages of the traditional CS method with the powerful learning ability of CNN. Besides, the projection operation only reuses the learned measurement matrices and the linear mapping matrices to update the image blocks. Thus, it does not introduce any extra parameters. As shown in Table IV, when removing the projection operation, the average reconstruction PSNR scores of our model

TABLE V THE INFLUENCE OF THE DEEP RECONSTRUCTION MODULE ON RECONSTRUCTION PERFORMANCE. THE TESTING SET IS SET11

		Sampling R	atio (PSNR)
Methods	0.01	0.1	0.3	0.5
CSNet ⁺ [14]	21.06	28.66	34.65	38.93
AMS-CSNet ⁺	20.59	28.99	34.93	38.14
SCSNet [16]	21.11	28.66	34.63	39.04
AMS-SCSNet	20.59	28.79	34.56	37.72
AMS-NoProj	20.79	29.12	34.71	37.84
AMS-Net	21.65	31.23	37.46	41.05

will degrade about $0.9 \sim 3$ dB on each sampling ratio. This demonstrates the effectiveness of the projection operation for image reconstruction.

3) Deep Reconstruction Module: To demonstrate the effectiveness of our deep reconstruction module, we construct two new models, the AMS-CSNet⁺ and AMS-SCSNet, by replacing the deep reconstruction module of our AMS-Net with the deep reconstruction module in CSNet⁺ [14] and SCSNet [16], respectively. Table V shows the comparison results on Set11 and the suffix "-NoProj" means that no projection operation is used in each reconstruction stage. As can be seen from Table V, the performance of the AMS-CSNet⁺ and AMS-SCSNet are not superior compared to the original models. Besides, with more convolutional layers, the AMS-NoProj achieves similar reconstruction performance with the AMS-CSNet⁺ and AMS-SCSNet, which indicates that the reconstruction performance cannot be improved by simply stacking more convolutional layers. Compared to other models, the proposed AMS-Net with projection operation can significantly improve the reconstruction performance. This demonstrates that the projection operation is very important for our adaptive multi-scale sampling model.

4) Reconstruction Stages: The reconstruction module of our AMS-Net has multiple reconstruction stages T. To evaluate the influence of T, we train the AMS-Net with multiple reconstruction stages ranging from 4 to 12. As can be seen from Table IV, the reconstruction quality can be improved with the increasing of T. However, when T > 10, the model appears to be over-fitting and slightly declines in the reconstruction performance. Thus, to achieve a relatively high reconstruction quality, we set T = 10 in our model.

5) LSRA Strategy: Considering that the block sparsities of the two groups of sub-bands in the wavelet domain are distributed unevenly, our model adaptively allocates sampling resources to different image blocks of the two groups of sub-bands using the LSRA strategy. As can be seen from the fourth row and the penultimate row of Table IV, the average reconstruction PSNR scores of the proposed model can improve about $0.5 \sim 3$ dB on each sampling ratio when using the LSRA strategy. This proves the effectiveness of the LSRA strategy on reconstruction performance.

6) Allocation Ratio: The allocation ratio ar is used to adaptively assign sampling resources according to the target sampling ratio. To test the influence of the ar on reconstruction performance, we train the AMS-Net with different settings of ar. The maximum value of ar is ranging from 0.65 to 0.95, and Table VI

TABLE VI THE INFLUENCE OF THE ALLOCATION RATIO *ar* ON RECONSTRUCTION QUALITY. THE TESTING SET IS SET11

Max an		Sampling Ratio	(PSNR/SSIM)	
Max. ar	0.01	0.1	0.3	0.5
0.95	21.65/0.5795	31.23/0.8867	37.46/0.9599	41.05/0.9770
0.85	21.38/0.5667	31.24/0.8839	37.59/0.9585	40.73/0.9745
0.75	21.26/0.5650	31.19/0.8816	37.48/0.9566	39.86/0.9709
0.65	21.14/0.5609	31.03/0.8780	37.16/0.9544	38.29/0.9653

TABLE VIIModel Complexity Comparisons of Different CS Methods With nSampling Ratios. The PN1 and PN2 are the Parameter Numbers of
the Learnable Matrices and All Other Convolutional Layers,
Respectively, and $SR = sr_1 + sr_2 + \dots + sr_n$ is the Sum of the n
Sampling Ratios

Methods	Scalable	PN_1	PN_2	FLOPs	Time
wiethous	Sampling	(M)	(M)	(G)	(s)
DAMP [33]	True	-	-	-	8.231
FOCUSS [13]	True	-	-	-	2.254
MH [34]	True	-	-	-	3.743
TV [11]	True	-	-	-	0.533
BCS-SPL [21]	True	-	-	-	1.506
MS-BCS [12]	True	-	-	-	0.910
ReconNet [23]	False	$1.05 \times SR$	0.02 imes n	3.2	0.002
CSNet ⁺ [14]	False	$2.10 \times SR$	$0.37 \times n$	6.82	0.005
ISTA-Net [37]	False	$1.05 \times SR$	$0.34 \times n$	37.12	0.008
AMP-Net [15]	False	$2.10 \times SR$	$0.34 \times n$	22.42	0.017
ISTA-Net ⁺⁺ [38]	True	-	0.76	49.45	0.015
SCSNet [16]	True	2.10	1.41	11.62	0.003
MSRNet [17]	False	$2.10 \times SR$	$2.05 \times n$	268.8	0.011
DoC-DCS [19]	False	$2.10 \times SR$	$16.29 \times n$	82.53	0.017
AMS-Net-T4	True	1.31	0.45	29.31	0.005
AMS-Net-T6	True	1.31	0.67	43.95	0.008
AMS-Net-T8	True	1.31	0.89	58.60	0.010
AMS-Net-T10	True	1.31	1.12	73.25	0.011

shows the comparison results. As can be seen, our model can get relatively high PSNR and SSIM scores when the maximum value of ar is 0.95. Thus, we set the maximum value of ar to 0.95 in the experiment settings.

E. Model Complexity

This section compares the model complexity of different CS methods in terms of parameter capacity and time complexity. The average running time is used to evaluate the actual reconstruction efficiency. Besides, we use the number of floating-point operations (FLOPs) [41] to quantify the time complexity, since it is commonly used in the time complexity comparison of deep learning-based models [6]. Note that the average running time and the number of FLOPs are calculated by reconstructing an image of size 256×256 . The traditional CS methods are implemented in MATLAB software and run on CPU, while the deep learning-based methods are tested on GPU. Table VII shows the comparison results and the suffix "T-" of our AMS-Net represents the number of reconstruction stages. As the DoC-DCS [19], P-DCI [20], SS-DCI [20] and MS-DCSNet [18] have the same reconstruction architecture, we only list the results of DoC-DCS [19] for comparison.

1) Parameter Capacity: As can be seen from Table VII, the SCSNet [16], ISTA-Net⁺⁺ [38] and our AMS-Net use scalable sampling strategies and train only one model for multiple sampling ratios, which significantly reduce the parameter capacity and training time. In contrast, all other models need to train a model for each sampling ratio. However, a method should be available for different sampling ratios. Thus, when performing tasks with *n* sampling ratios, they need to train *n* models for these *n* sampling ratios, which greatly increases the parameter capacity and training time. As a result, for a normal task (e.g., n > 10), our AMS-Net can achieve the second smallest parameter capacity and only has larger parameter capacity than ISTA-Net⁺⁺ [38]. Thus, our AMS-Net can achieve a small parameter capacity while keeping the best reconstruction

2) *Time Complexity:* As shown in Table VII, it takes several seconds for traditional CS methods to reconstruct the images, while the average running times for deep learning-based methods are below 0.1 seconds when running on GPU. This is because the reconstruction process of traditional CS methods is implemented iteratively until achieving convergence or reaching the maximum iteration steps. Besides, compared with CPU, the GPU has advantages in calculation ability and parallel computation. This can heavily reduce the running time of the deep learning-based CS methods.

Among all the deep learning-based CS methods, the Recon-Net [23] has the least FLOPs but the lowest reconstruction quality (see Table III), because it has fewer convolutional layers than other models. Our model has a comparative number of FLOPs compared to other models. Besides, with a small number of reconstruction stages, our AMS-Net can achieve a faster reconstruction speed and less FLOPs while maintaining a good reconstruction performance (see Table IV). In general, these deep learning-based CS methods have different time complexity. However, due to the strong computation efficiency of GPU, the slightly different running times of these methods do not make much sense. Since all running speeds are almost the same magnitude, the reconstruction quality is more important for a deep learning-based method. Our AMS-Net can achieve better reconstruction quality than other methods, especially at low sampling ratios (see Table III and Fig. 6).

VI. CONCLUSION

In this paper, we proposed a dual-channel deep network for adaptive multi-scale image CS, called AMS-Net, which fully exploits the different importance of the image low-frequency and high-frequency components in the wavelet domain. An original image is decomposed into four sub-images using the DWT, namely the LL, LH, HL and HH sub-bands. Since the LL sub-band is low-frequency components and more important to the reconstruction quality than the other three sub-bands, the AMS-Net allocates the LL sub-band a larger sampling ratio while allocating the other three sub-bands a smaller one. Considering the different sparsity in different blocks, an LSRA strategy is proposed to further adjust the sampling resources block-by-block on the two groups of sub-bands, respectively. Then a dual-channel scalable sampling model is developed to apply adaptive sampling tasks in the wavelet domain at arbitrary sampling ratios. Furthermore, by unfolding the reconstruction process of the traditional multi-scale block CS algorithm, we propose a multi-stage reconstruction architecture to utilize multi-scale features for further enhancing the reconstruction quality. Comparison results demonstrate that our AMS-Net can outperform the traditional CS methods and state-of-the-art deep leaning-based CS methods.

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Kuiyuan Zhang received the M.S. degree in computer science and technology from the Harbin Institute of Technology, Shenzhen, Shenzhen, China, where he is currently working toward the Ph.D degree in computer science and technology. His research interests include image compressive sensing and image encryption.



Zhongyun Hua (Member, IEEE) received the B.S. degree in software engineering from Chongqing University, Chongqing, China, in 2011, and the M.S. and Ph.D. degrees in software engineering from the University of Macau, Macau, China, in 2013 and 2016, respectively. He is currently an Associate Professor with the School of Computer Science and Technology, Harbin Institute of Technology, Shenzhen, Shenzhen, China. He has authored or coauthored more than 50 papers on the subject, receiving more than 3500 citations. His research interests include chaotic sys-

tem, image processing, and multimedia security. He is currently an Associate Editor for the *International Journal of Bifurcation and Chaos*.



Yuanman Li (Member, IEEE) received the B.Eng. degree in software engineering from Chongqing University, Chongqing, China, in 2012, and the Ph.D. degree in computer science from the University of Macau, Macau, China, in 2018. From 2018 to 2019, he was a Postdoctoral Fellow with the State Key Laboratory of Internet of Things for Smart City, University of Macau. He is currently an Assistant Professor with the College of Electronics and Information Engineering, Shenzhen University, Shenzhen, China. His research interests include data representation, multi-

media security and forensics, computer vision, and machine learning.



Yongyong Chen (Member, IEEE) received the B.S. and M.S. degrees from the Shandong University of Science and Technology, Qingdao, China, in 2014 and 2017, respectively, and the Ph.D. degree from the University of Macau, Macau, China, in 2020. He is currently an Assistant Professor with the School of Computer Science and Technology, Harbin Institute of Technology, Shenzhen, Shenzhen, China. He has authored or coauthored more than 30 research papers in top-tier journals and conferences, including IEEE TRANSACTIONS ON IMAGE PROCESSING,

IEEE TRANSACTIONS ON NEURAL NETWORKS AND LEARNING SYSTEMS, IEEE TRANSACTIONS ON MULTIMEDIA, IEEE TRANSACTIONS ON CIRCUITS AND SYS-TEMS FOR VIDEO TECHNOLOGY, IEEE TRANSACTIONS ON GEOSCIENCE AND REMOTE SENSING, IEEE TRANSACTIONS ON COMPUTATIONAL IMAGING, IEEE JOURNAL OF SELECTED TOPICS IN SIGNAL PROCESSING, Pattern Recognition and ACM MM. His research interests include image processing, data mining, and computer vision.



Yicong Zhou (Senior Member, IEEE) received the B.S. degree in electrical engineering from Hunan University, Changsha, China, and the M.S. and Ph.D. degrees in electrical engineering from Tufts University, Medford, MA, USA. He is a Professor with the Department of Computer and Information Science, University of Macau, Macau, China. His research interests include image processing, computer vision, machine learning, and multimedia security. He is a Fellow of SPIE the Society of Photo-Optical Instrumentation Engineers) and was recognized as one of

World's Top 2% Scientists and one of Highly Cited Researchers in 2020 and 2021. He was the recipient of the Third Price of Macao Natural Science Award as a sole winner in 2020 and a co-recipient in 2014. Dr. Zhou has been a leading Co-Chair of Technical Committee on Cognitive Computing in the IEEE SYS-TEMS, *Man*, and Cybernetics Society since 2015. He is an Associate Editor for the IEEE TRANSACTIONS ON NEUTRAL NETWORKS AND LEARNING SYSTEMS, IEEE TRANSACTIONS ON CIRCUITS AND SYSTEMS FOR VIDEO TECHNOLOGY, IEEE TRANSACTIONS ON GEOSCIENCE AND REMOTE SENSING, and four other journals.